

New Vistas in High-Level Synthesis: Working with the Heap

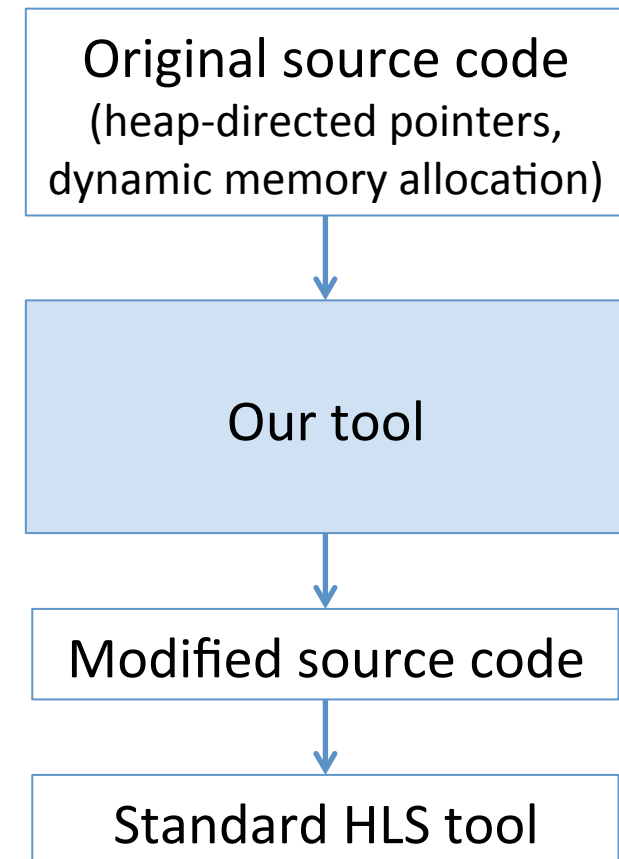
George A. Constantinides
(joint work with Winterstein)

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HLS for the Heap

Summary

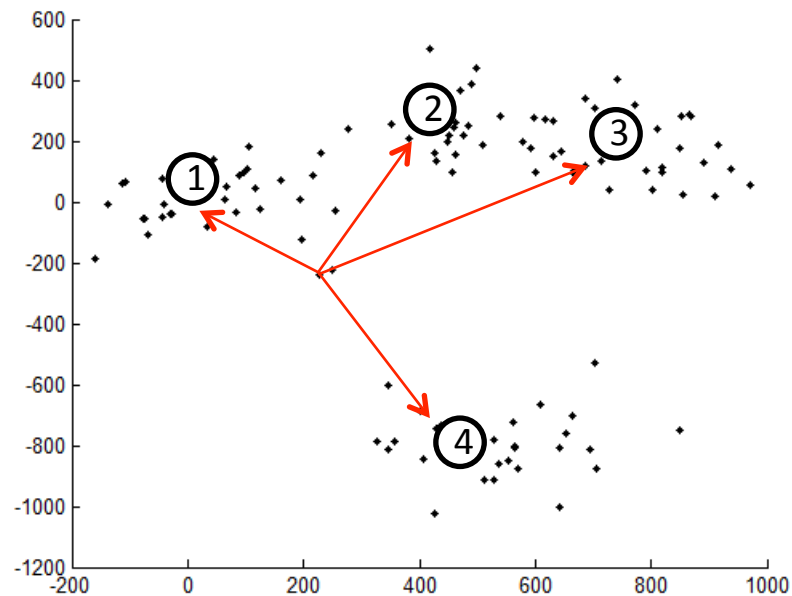
- HLS tools map code to hardware but require manual source code refactoring...
 - ... to map pointer-manipulating programs efficiently into HW
- A static program analysis
 - to analyse pointer-based memory accesses and heap layout
 - to identify disjoint, independent regions in heap memory
- Source-to-source transformations
 - to partition heap across on-chip memory banks
 - To perform automatic loop parallelization



- State-of-the-art HLS tools don't support full featured C/C++ code
- A major restriction: Heap directed pointers and dynamic memory allocation not supported
- **Worth considering at all?**

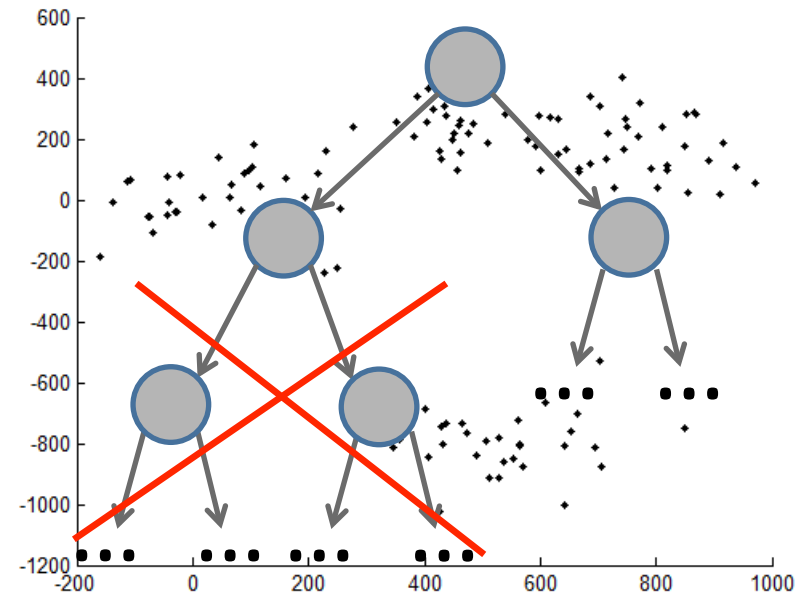
Case study:

- Compare computational properties of two algorithms for *K*-means clustering
- SW (C++) / RTL (VHDL) / HLS (C++) implementations
- Code available on GitHub (Vivado-KMeans)



Brute-force algorithm

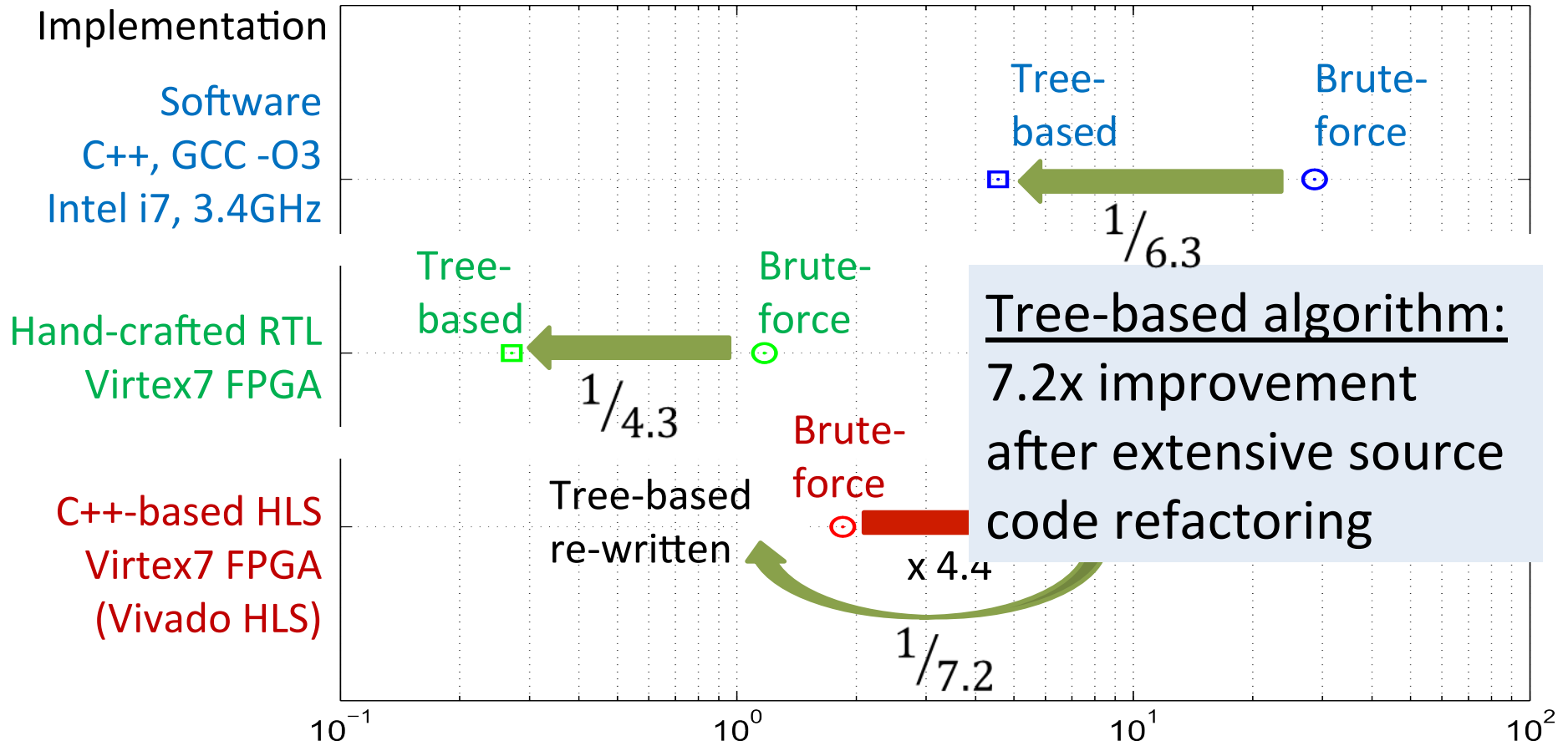
- Computationally expensive
- Simple control flow
- Embarrassingly parallel



Tree-based algorithm

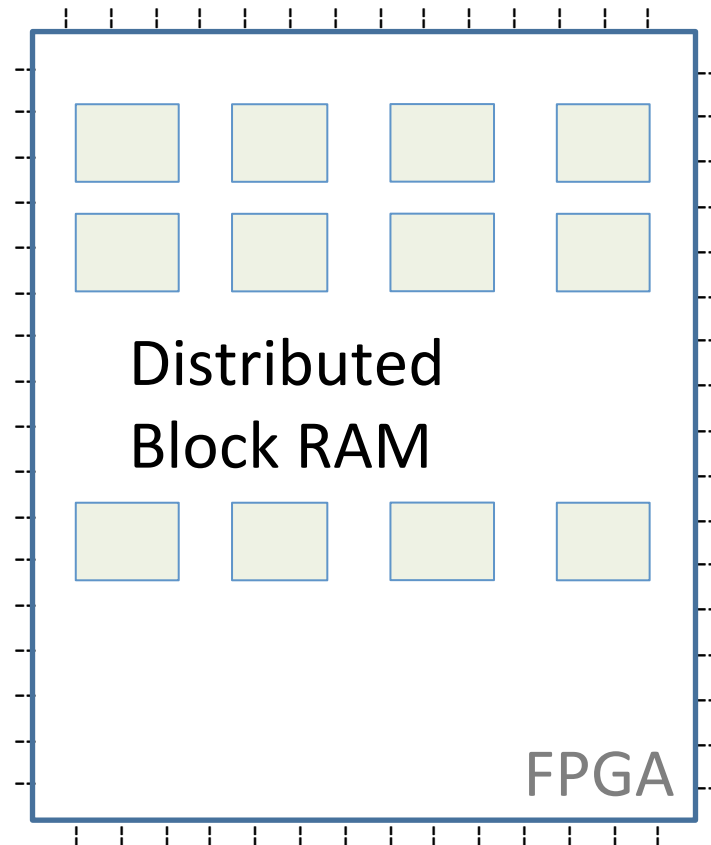
- Data-dependent control flow
- Pointer-based tree traversal
- Dynamic memory allocation

The battlefield



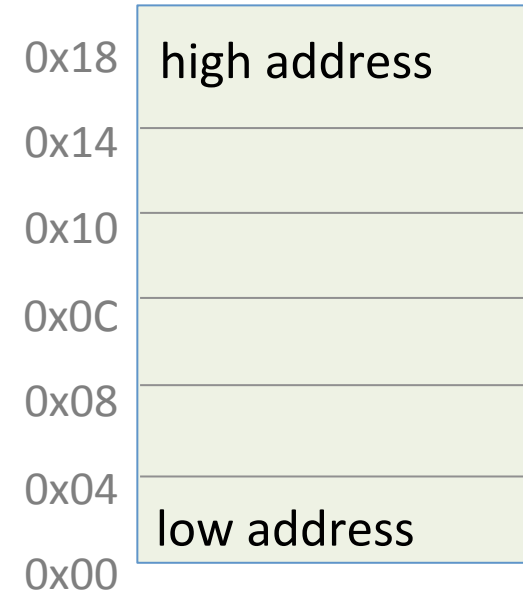
Tree-based algorithm:
7.2x improvement
after extensive source
code refactoring

Identical area constraint for FPGA implementations: 6500 slices



HLS
←

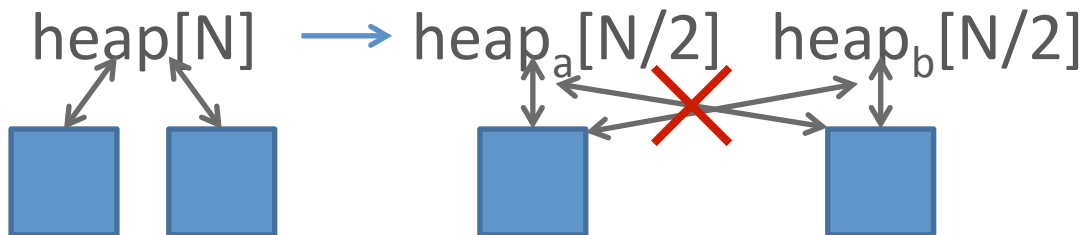
SW memory model



```
int main() {  
    x = A[i];  
    p = new int;  
    *p = 3;  
    ...  
}
```

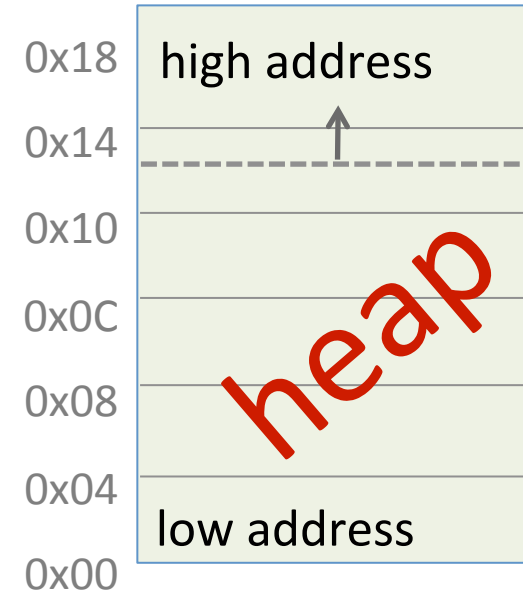
Our goal

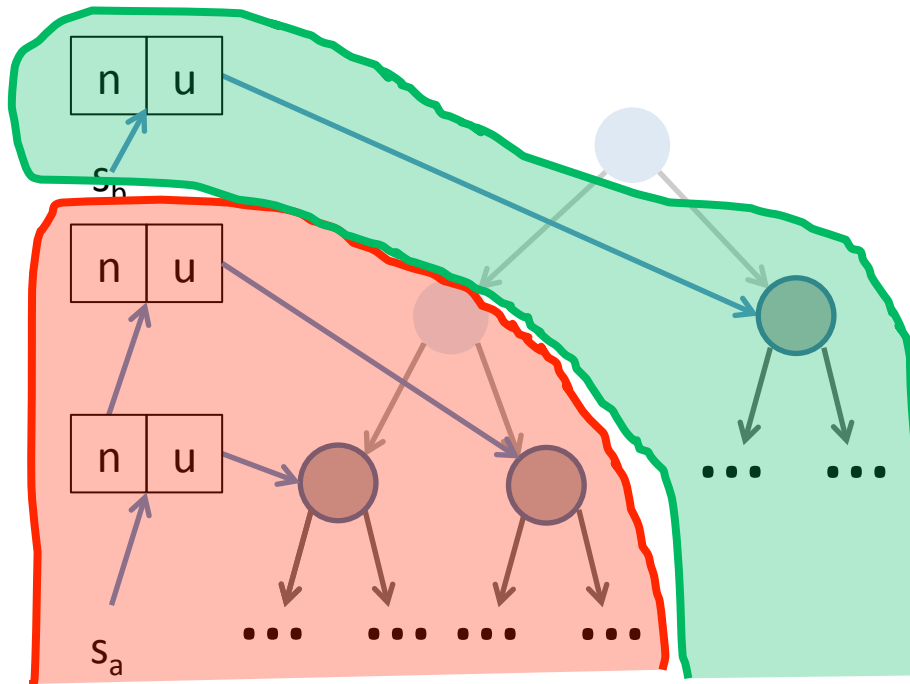
- Partition heap-allocated data structures ('heaplets')
- Synthesize a parallel implementation



- Ensure that heap partitions are 'private'

SW memory model



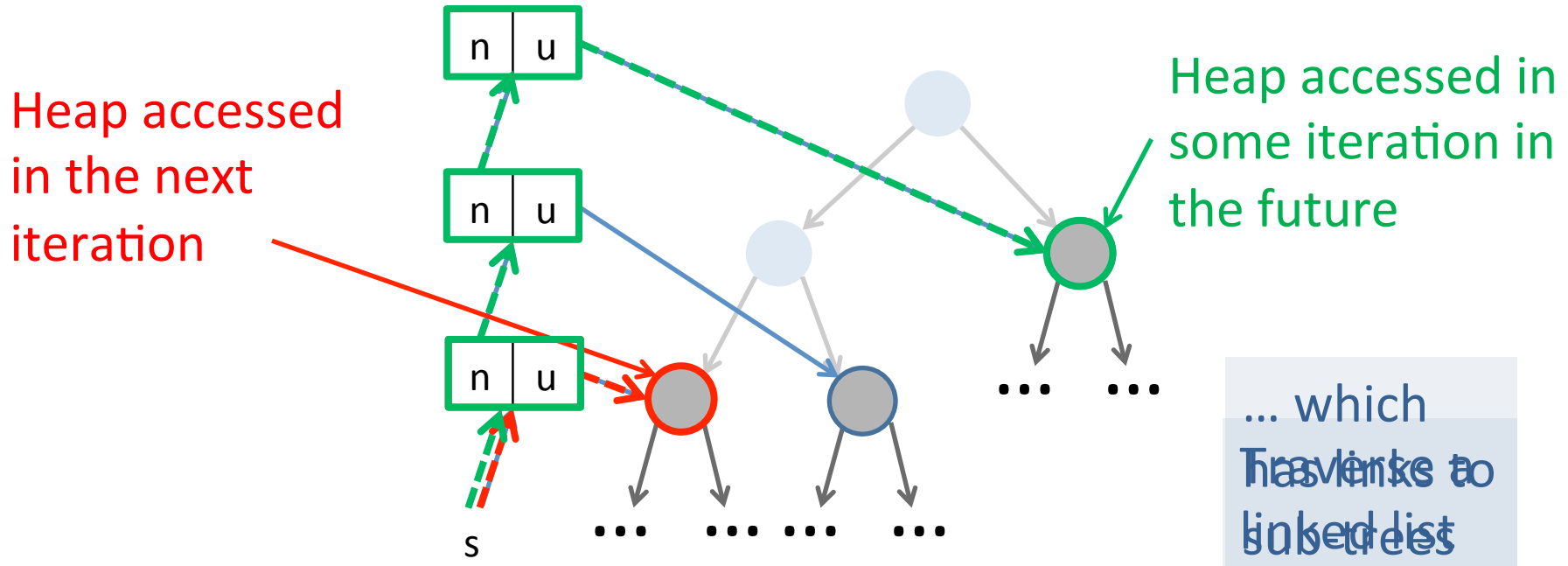


```

s := PUSH(n, s); // accessing root node
while s != 0 do
  while POP(&u, s);
    ... loop body (access left sub-tree)
  end while;
  if (u->left != 0) && (u->right != 0) then
    s = PUSH(u->right, s);
    while s != 0 do
      ... loop body (access right sub-tree)
    end while;
  end if;
end while;
end while;
end while

```

- Partition linked list and tree
- Will the **red loop** ever access data in the **green partition**? No!
- Parallelization is legal (does not violate data dependencies)
- Why is it hard for a tool to figure this out?

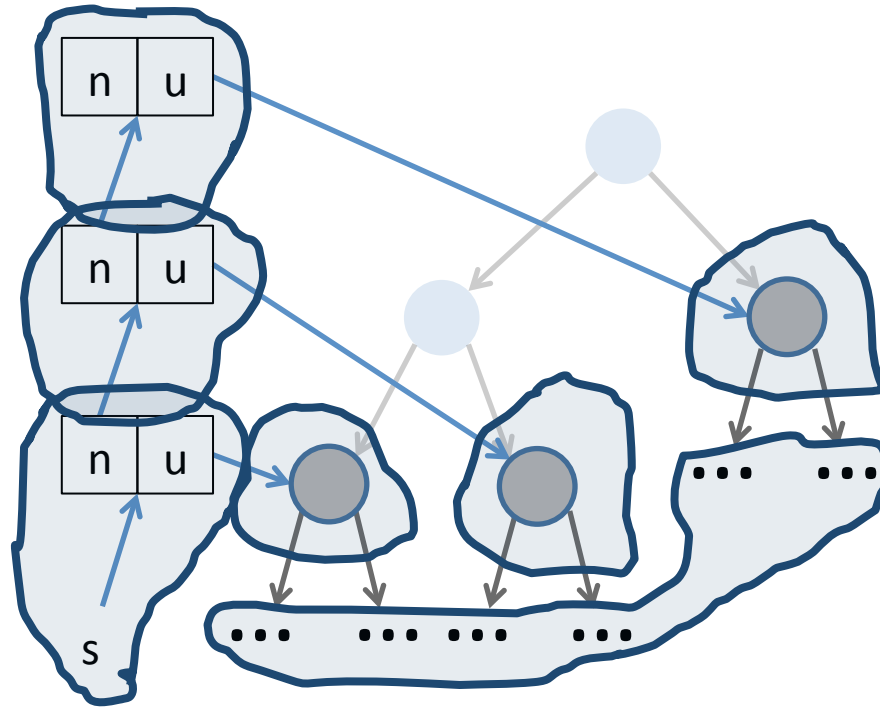


- Do these iterations access the same memory cell?

$$\text{heap}[\text{heap}[s].u] = ? \text{heap}[\text{heap}[\text{heap}[\text{heap}[\text{heap}[s].h].h].h].u]$$

- Need to reason about structure, heap layout and disjointness
- None of this is explicit in the above representation

Describe heap layout with formulae



Conjunction
' \wedge ' does not
rule out
aliasing!

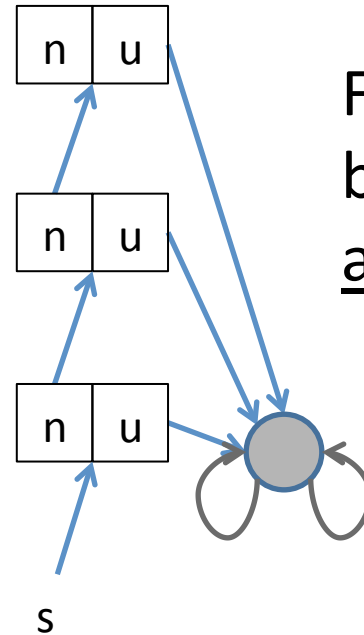
$$\underbrace{s \rightarrow [u: u'_1, n: s'_1]}_{\wedge} \wedge \underbrace{s'_1 \rightarrow [u: u'_2, n: s'_2]}_{\wedge} \wedge s'_2 \rightarrow [u: u'_3, n: 0]$$

"s points to a record with fields u and n"

$$\wedge u'_1 \rightarrow [l: u'_4, r: u'_5] \wedge u'_3 \rightarrow [l: u'_8, r: u'_9] \wedge u'_2 \rightarrow [l: u'_6, r: u'_7]$$

$$\wedge \dots$$

Describe heap
layout with
formulae

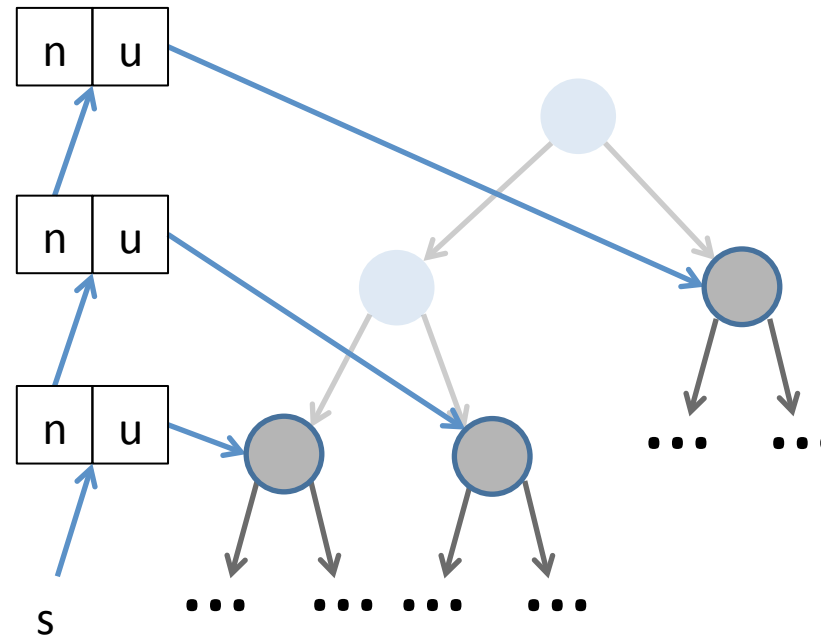


Formula
below can
also mean this

Conjunction
' \wedge ' does not
rule out
aliasing!

$$\begin{aligned}
 & s \rightarrow [u: u'_1, n: s'_1] \wedge s'_1 \rightarrow [u: u'_2, n: s'_2] \wedge s'_2 \rightarrow [u: u'_3, n: 0] \\
 & \wedge u'_1 \rightarrow [l: u'_4, r: u'_5] \wedge u'_3 \rightarrow [l: u'_8, r: u'_9] \wedge u'_2 \rightarrow [l: u'_6, r: u'_7] \\
 & \wedge \dots
 \end{aligned}$$

Describe heap
layout with
formulae

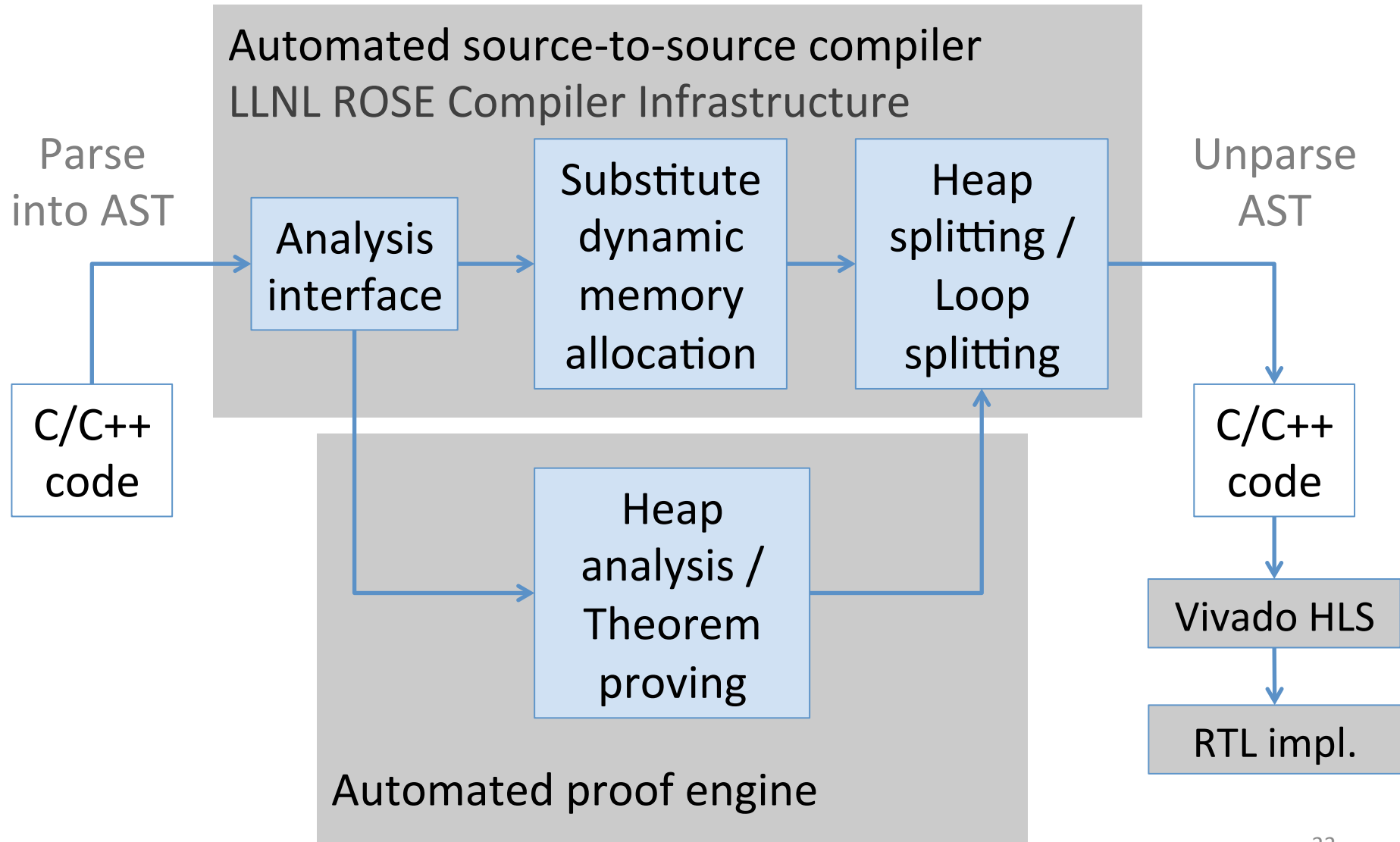


- Tractable heap analysis
- Task: Split the heap formula into red and green partition

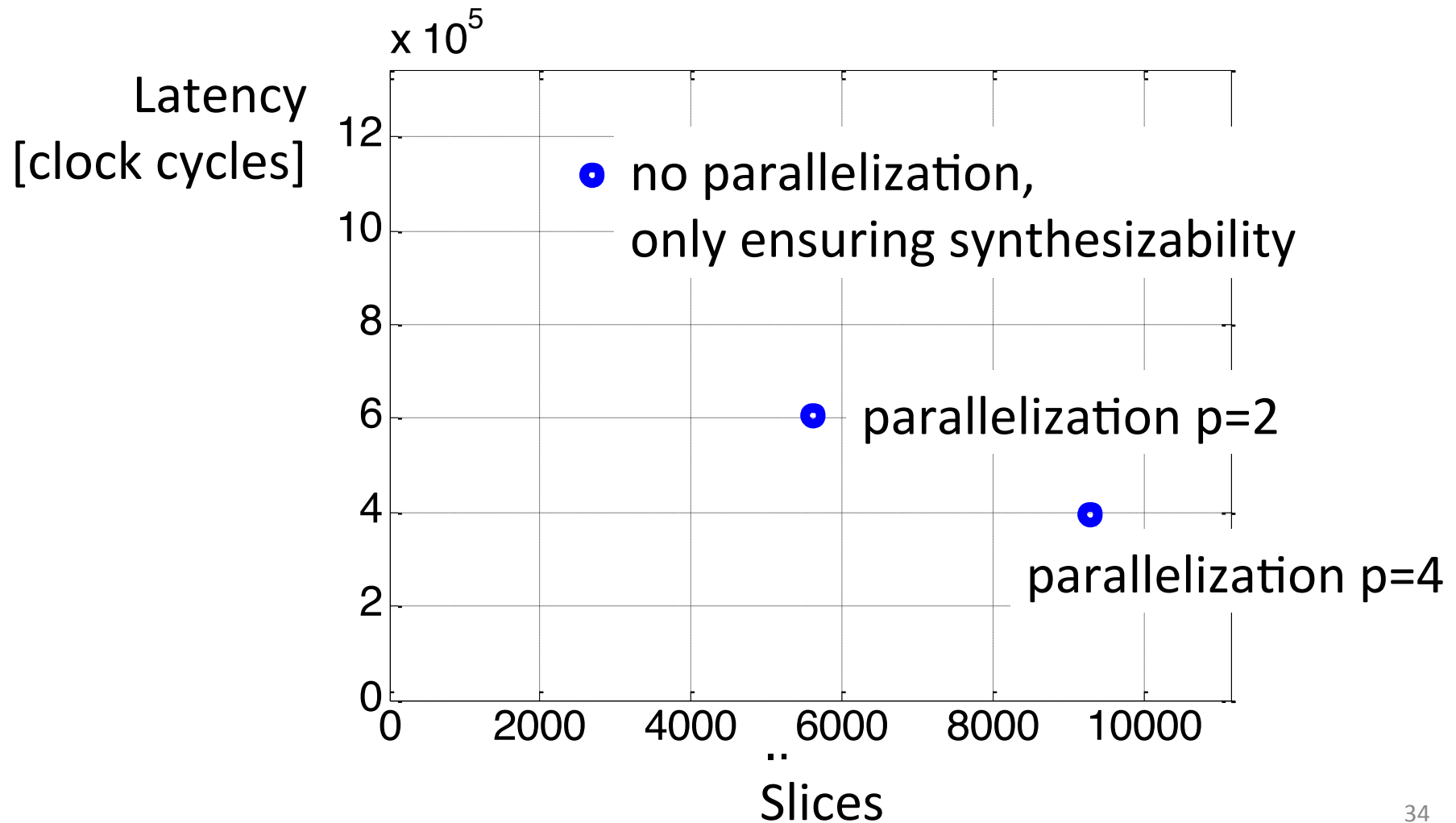
$$\begin{aligned}
 & s \rightarrow [u: u'_1, n: s'_1] * s'_1 \rightarrow [u: u'_2, n: s'_2] * s'_2 \rightarrow [u: u'_3, n: 0] \\
 & * u'_1 \rightarrow [l: u'_4, r: u'_5] * u'_3 \rightarrow [l: u'_8, r: u'_9] * u'_2 \rightarrow [l: u'_6, r: u'_7]
 \end{aligned}$$





- Symbolically execute the program using (a modified version of) *coreStar*

$$\begin{array}{l}
 \{ x = y'_1 \} \quad x := E \quad \{ x = E[y'_1/x] \} \\
 \{ E \mapsto [f : y'_1] \} \quad [E].f := F \quad \{ E \mapsto [f : F] \} \\
 \{ x = y'_1 \wedge E \mapsto [f : z'_1] \} \quad x := [E].f \quad \{ x = z'_1 \wedge E[y'_1/x] \mapsto [f : z'_1] \} \\
 \{ emp \} \quad new(x) \quad \{ x \mapsto z'_1 \} \\
 \{ E \mapsto y' \} \quad delete(E) \quad \{ emp \}
 \end{array}$$



Tree-based *K*-means clustering



	P	Slices	Clock	Cycles	
1 Merger (linked lists)					
Baseline (no par.)	1	574	9.0 ns	21167k	 x4
Autom. Parallelization	4	965	8.7 ns	5483k	
2 Tree deletion (tree, linked list)					
Baseline (no par.)	1	1521	5.2 ns	901k	 x2
Autom. Parallelization	2	4069	6.0 ns	487k	
3 K-means (tree, linked list, single heap records)					
Baseline (no par.)	1	2694	6.1 ns	1120k	 x2
Autom. Parallelization	2	5618	7.0 ns	606k	
					 x3.6

Conclusions

- Exciting issues in HLS
 - Memory
 - Heap, Arrays
 - Real arithmetic (come to another talk!)
- Lots still to do
 - Unified theoretical basis for memory optimisation
 - Scope for SVM support and fancy memory models
 - Incorporation of non-traditional error sources
 - ...

Thank you for listening.